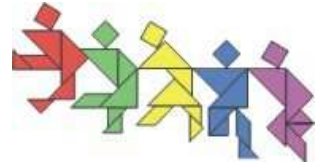






# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



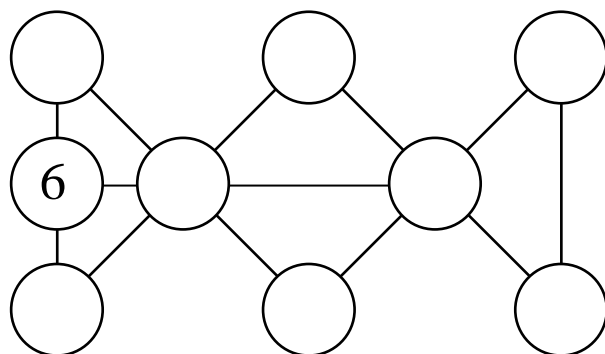
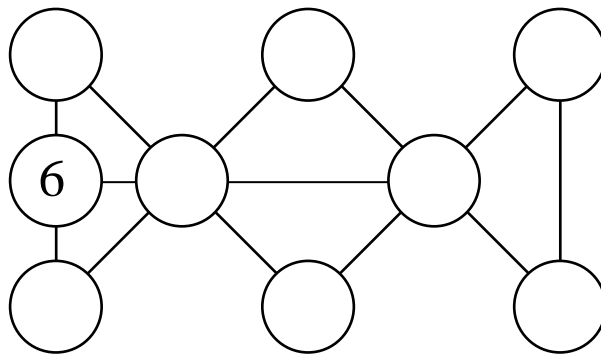
## *Elementary Mathematics International Contest*

### TEAM CONTEST

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

- Each of the nine circles in the diagram below contains a different positive integer. These integers are consecutive and the sum of numbers in all the circles on each of the seven lines is 23. The number in the circle at the top right corner is less than the number in the circle at the bottom right corner. Eight of the numbers have been erased. Restore them.



Answer: \_\_\_\_\_



# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



## *Elementary Mathematics International Contest*

# TEAM CONTEST

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

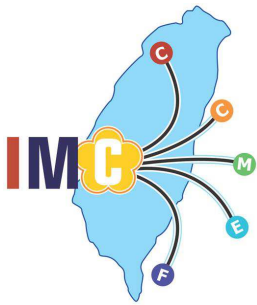
2. A clay tablet consists of a table of numbers, part of which is shown in the diagram below on the left. The first column consists of consecutive numbers starting from 0. In the first row, each subsequent number is obtained from the preceding one by adding 1. In the second row, each subsequent number is obtained from the preceding one by adding 2. In the third row, each subsequent number is obtained from the preceding one by adding 3, and so on. The tablet falls down and breaks up into pieces, which are swept away except for the two shown in the diagram below on the right in magnified forms, each with a smudged square. What is the sum of the two numbers on these two squares?

0	1	2	3	4	5	
1	3	5	7	9	11	
2	5	8	11	14	17	
3	7	11	15	19	23	
4	9	14	19	24	29	
5	11	17	23	29	35	

?	2012	2023
---	------	------

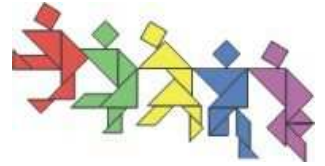
2012
2683
?

Answer: \_\_\_\_\_



# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



## *Elementary Mathematics International Contest*

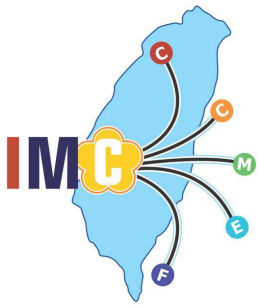
### TEAM CONTEST

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

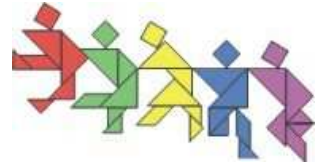
3. In a row of numbers, each is either 2012 or 1. The first number is 2012. There is exactly one 1 between the first 2012 and the second 2012. There are exactly two 1s between the second 2012 and the third 2012. There are exactly three 1s between the third 2012 and the fourth 2012, and so on. What is the sum of the first 2012 numbers in the row?

Answer: \_\_\_\_\_



**Taiwan International  
Mathematics Competition 2012  
(TAIMC 2012)**

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



*Elementary Mathematics International Contest*

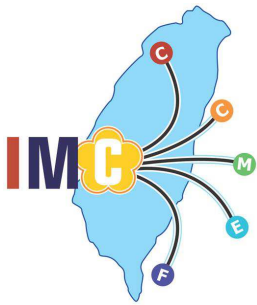
**TEAM CONTEST**

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

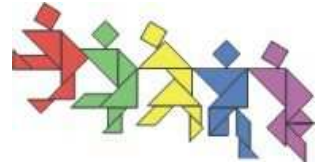
4. In a test, one-third of the questions were answered incorrectly by Andrea and 7 questions were answered incorrectly by Barbara. One fifth of the questions were answered incorrectly by both of them. What was the maximum number of questions which were answered correctly by both of them?

Answer: \_\_\_\_\_



**Taiwan International  
Mathematics Competition 2012  
(TAIMC 2012)**

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



*Elementary Mathematics International Contest*

**TEAM CONTEST**

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

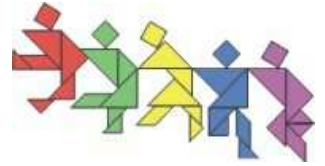
5. Five different positive integers are multiplied two at a time, yielding ten products. The smallest product is 28, the largest product is 240 and 128 is also one of the products. What is the sum of these five numbers?

Answer: \_\_\_\_\_



# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



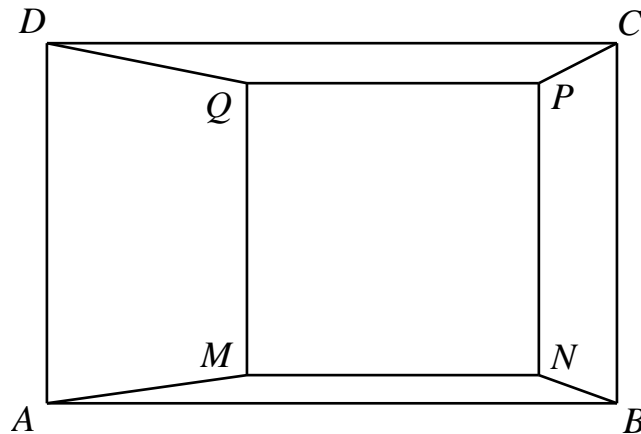
## *Elementary Mathematics International Contest*

### TEAM CONTEST

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

6. The diagram below shows a square  $MNPQ$  inside a rectangle  $ABCD$  where  $AB - BC = 7$  cm. The sides of the rectangle parallel to the sides of the square. If the total area of  $ABNM$  and  $CDQP$  is  $123$   $\text{cm}^2$  and the total area of  $ADQM$  and  $BCPN$  is  $312$   $\text{cm}^2$ , what is the area of  $MNPQ$  in  $\text{cm}^2$ ?

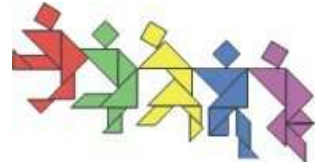


Answer: \_\_\_\_\_  $\text{cm}^2$



# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



## *Elementary Mathematics International Contest*

### **TEAM CONTEST**

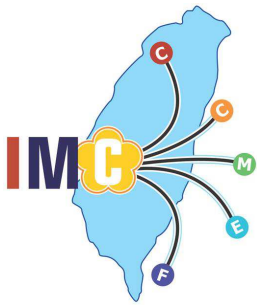
25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

7. Two companies have the same number of employees. The first company hires new employees so that its workforce is 11 times its original size. The second company lays off 11 employees. After the change, the number of employees in the first company is a multiple of the number of employees in the second company. What is the maximum number of employees in each company before the change?

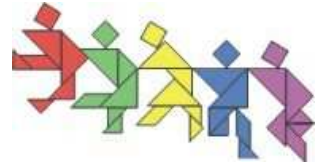
Answer: \_\_\_\_\_





# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



## *Elementary Mathematics International Contest*

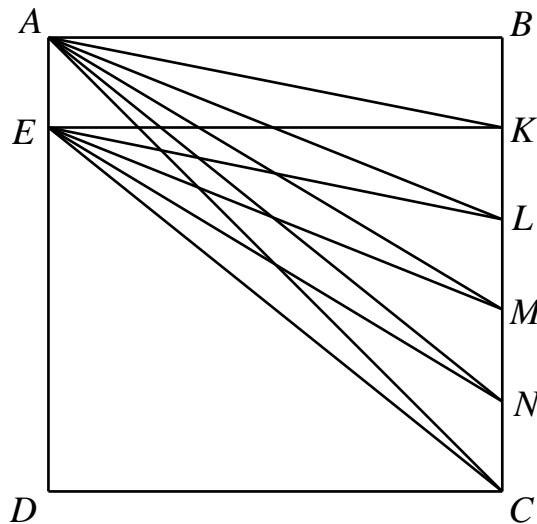
### TEAM CONTEST

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

8.  $ABCD$  is a square.  $K, L, M$  and  $N$  are points on  $BC$  such that  $BK = KL = LM = MN = NC$ .  $E$  is the point on  $AD$  such that  $AE = BK$ . In degrees, what is the measure of

$$\angle AKE + \angle ALE + \angle AME + \angle ANE + \angle ACE ?$$



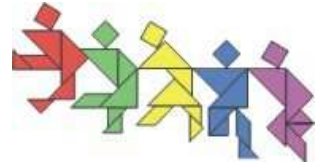
○

Answer: \_\_\_\_\_



# Taiwan International Mathematics Competition 2012 (TAIMC 2012)

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



## *Elementary Mathematics International Contest*

### TEAM CONTEST

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

9. The numbers 1 and 8 have been put into two squares of a  $3 \times 3$  table, as shown in the diagram below. The remaining seven squares are to be filled with the numbers 2, 3, 4, 5, 6, 7 and 9, using each exactly once, such that the sum of the numbers is the same in any of the four  $2 \times 2$  subtables shaded in the diagram below. Find all possible solutions.

1		
		8

1		
		8

1		
		8

1		
		8

1		
		8

1		
		8

1		
		8

1		
		8

1		
		8

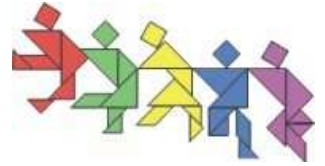
1		
		8

Answer: \_\_\_\_\_



**Taiwan International  
Mathematics Competition 2012  
(TAIMC 2012)**

World Conference on the Mathematically Gifted Students  
---- the Role of Educators and Parents  
Taipei, Taiwan, 23rd~28th July 2012



*Elementary Mathematics International Contest*

**TEAM CONTEST**

25<sup>th</sup> July 2012 Taipei, Taiwan

Team : \_\_\_\_\_ Score : \_\_\_\_\_

10. At the beginning of each month, an adult red ant gives birth to three baby black ants. An adult black ant eats one baby black ant, gives birth to three baby red ants, and then dies (Also, it is known that there are always enough baby black ants to be eaten.) During the month, baby ants become adult ants, and the cycle continues. If there are 9000000 red ants and 1000000 black ants on Christmas day, what was the difference between the number of red ants and the number of black ants on Christmas day a year ago?

Answer: \_\_\_\_\_